## Definitions and Formulas for Middle Level/Intermediate Mathematics

| Notation | Description |
| :---: | :---: |
| $a \rightarrow b$ | $a$ implies b |
| $a \leftrightarrow b$ | $a$ if and only if $b$ |
| $a \wedge b$ | $a$ and $b$ |
| $a \vee b$ | $a$ or $b$ |
| $\sim a$ | not a |
| $A \cup B$ | $A$ union $B$ |
| $A \cap B$ | $A$ intersect $B$ |
| $\bar{A}$ | complement of $A$ |
| $U$ | universal set |
| \{\} | empty set |
| $i=\sqrt{-1}$ | imaginary unit |
| $\bar{z}$ | complex conjugate of $z$ |
| $A^{-1}$ | inverse of matrix $A$ |
| $\stackrel{\rightharpoonup}{v}$ | vector $v$ |
| $\sim$ | is similar to |
| $\cong$ | is congruent to |
|  | congruent angles |
|  | congruent sides |
|  | parallel lines |


| Formula | Description |
| :---: | :---: |
| $V=\frac{1}{3} B h$ | volume of a right cone and a pyramid |
| $A=4 \pi r^{2}$ | surface area of a sphere |
| $V=\frac{4}{3} \pi r^{3}$ | volume of a sphere |
| $S_{n}=\frac{n}{2}[2 a+(n-1) d]=n\left(\frac{a+a_{n}}{2}\right)$ | sum of an arithmetic series |
| $S_{n}=\frac{a\left(1-r^{n}\right)}{1-r}$ | sum of a geometric series |
| $\sum_{n=0}^{\infty} a r^{n}=\frac{a}{1-r},\|r\|<1$ | sum of an infinite geometric series |
| $d=\sqrt{\left(x_{2}-x_{1}\right)^{2}+\left(y_{2}-y_{1}\right)^{2}}$ | distance formula |
| $\left(\frac{x_{1}+x_{2}}{2}, \frac{y_{1}+y_{2}}{2}\right)$ | midpoint formula |
| $m=\frac{\Delta y}{\Delta x}=\frac{y_{2}-y_{1}}{x_{2}-x_{1}}$ | slope |
| $y=a x^{2}+b x+c$ | parabola |
| $s^{2}=\frac{\sum_{i=1}^{n}\left(x_{i}-\bar{x}\right)^{2}}{n-1}$ | variance |
| $s=r \theta$ | arc length |
| $x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$ | quadratic formula |
| ${ }_{n} C_{r}=\frac{n!}{r!(n-r)!}$ | combinations |
| ${ }_{n} P_{r}=\frac{n!}{(n-r)!}$ | permutations |
| Formula | Description |
| $\sin \theta=\frac{o p p}{h y p}$ | sine of $\theta$ in a right triangle |
| $\cos \theta=\frac{\text { adj }}{\text { hyp }}$ | cosine of $\theta$ in a right triangle |
| $\tan \theta=\frac{\mathrm{opp}}{\mathrm{adj}}$ | tangent of $\theta$ in a right triangle |

